

Algebra 1.2

Chapter 12 Review

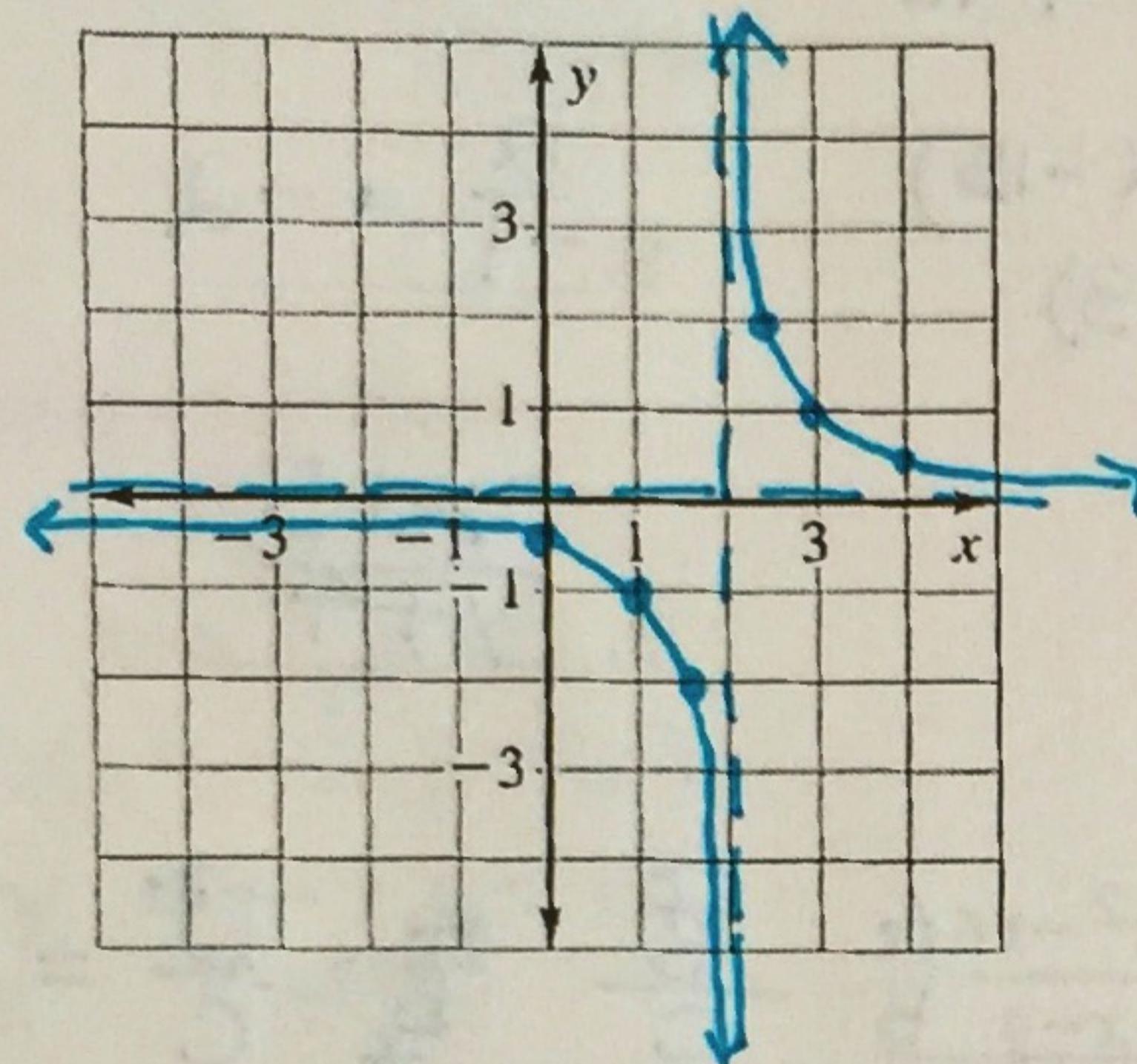
Name _____

State the domain and range, complete the table, and graph each rational equation.

1. $y = \frac{1}{x-2}$

Domain: ARNE 2 vRange: ARNE 0 +

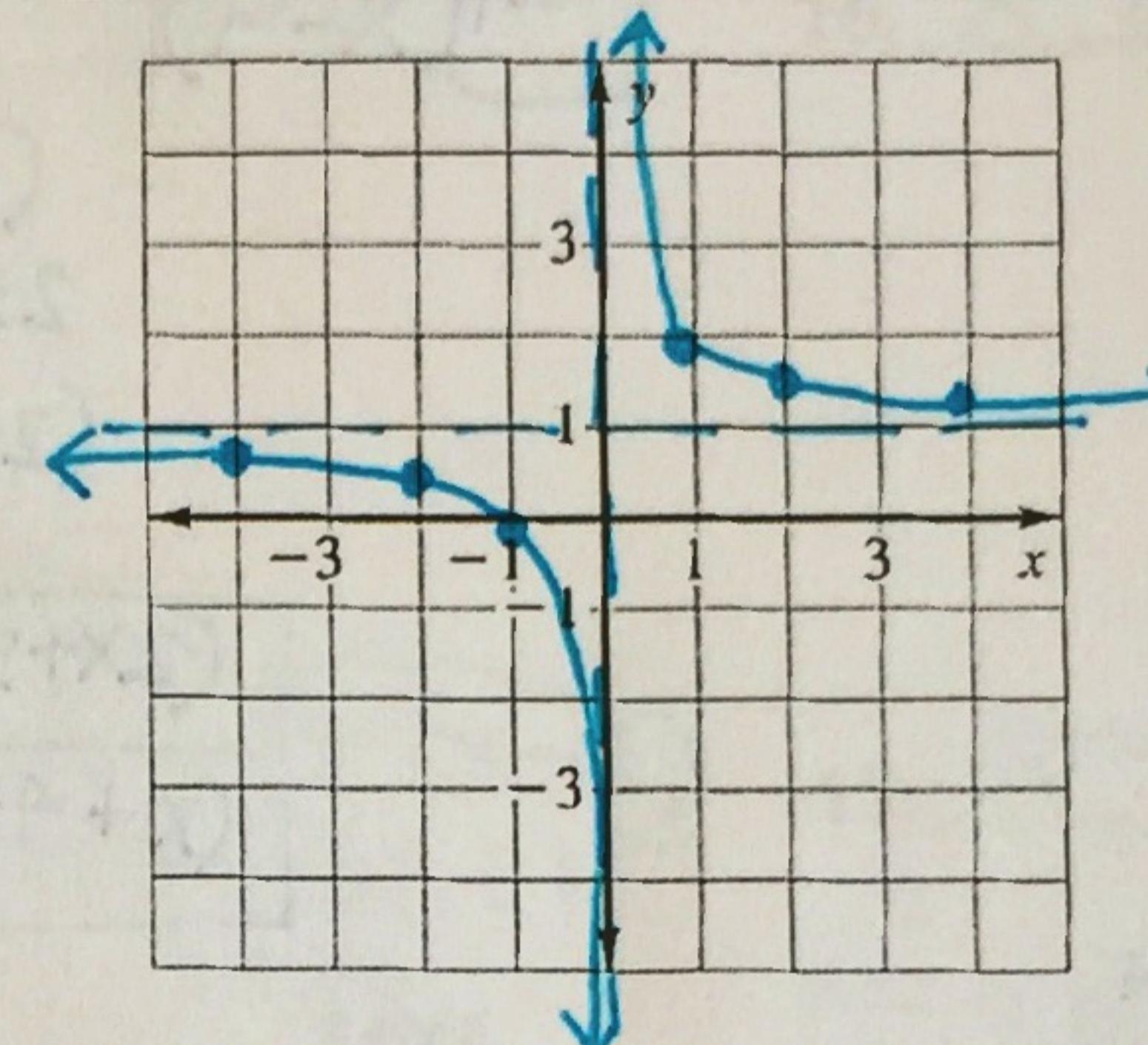
x	0	1	1.5	2	2.5	3	4
y	-1/2	-1	-2	2	1	1/2	



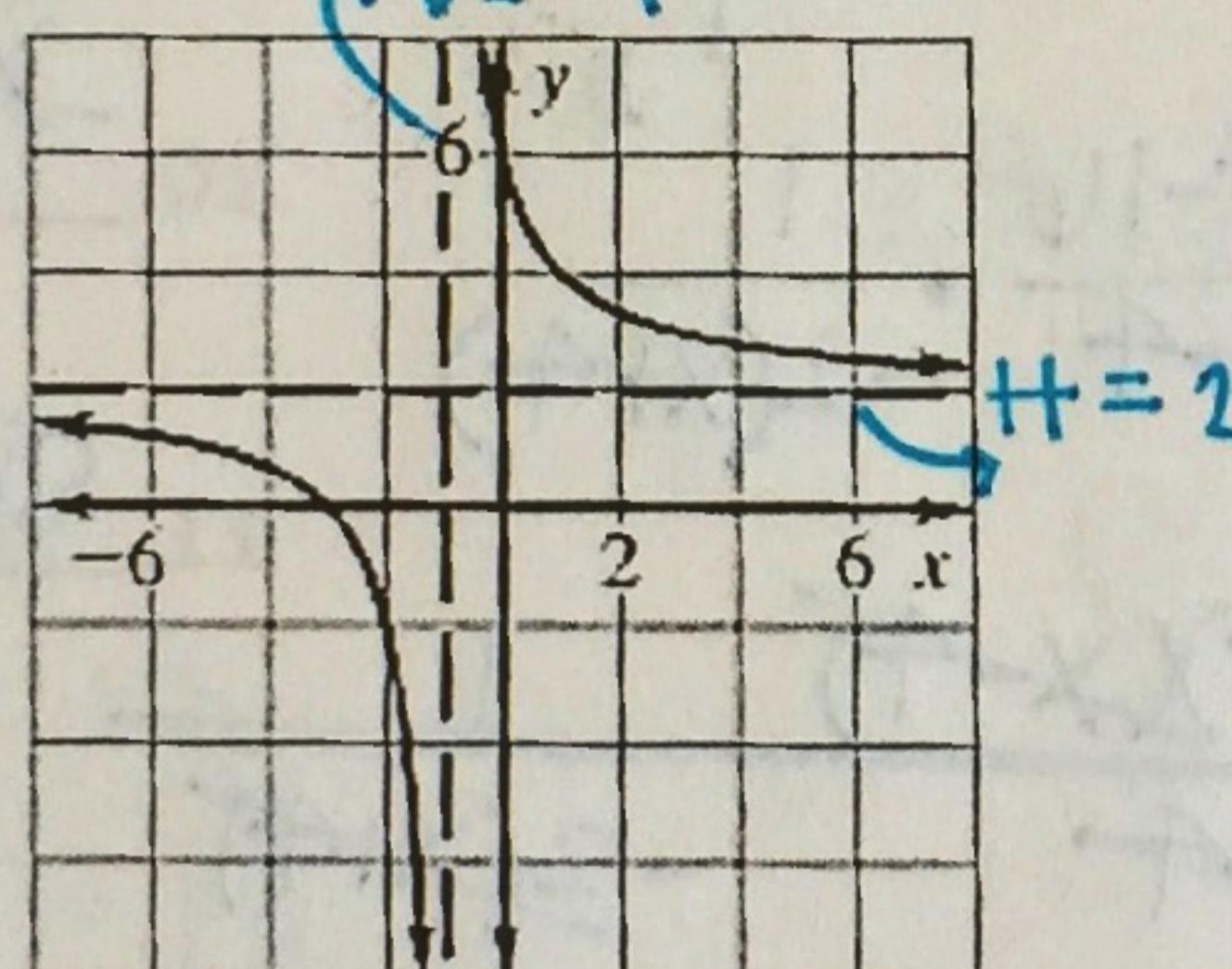
2. $y = \frac{1}{x} + 1$

Domain: ARNE 0 vRange: ARNE 1 +

x	-4	-2	-1	0	1	2	4
y	3/4	1/2	0	X	2	1 1/2	1 1/4



3. Which equation represents the given graph?



Domain V Range +

A. $y = \frac{4}{x+1} - 2$ + = -2

V = -1

B. $y = \frac{4}{x-1} - 2$ + = -2

V = 1

C. $y = \frac{4}{x+1} + 2$ + = 2

V = -1

D. $y = \frac{4}{x-1} + 2$ + = 2

V = 1

3. C.

Divide each. Show proper work!

4. $(18x^4 + 54x^2 - 6x) \div 6x$

$$\begin{array}{r} 3x^3 + 9x - 1 \\ \hline 6x \overline{)18x^4 + 54x^2 - 6x} \\ 18x^4 \\ \hline -54x^2 \\ -6x \\ \hline 0 \end{array}$$

5. $(x^2 + 3x - 6) \div (x + 1)$

$$\begin{array}{r} x+2 \\ \hline x+1 \overline{x^2 + 3x - 6} \\ x^2 \\ \hline -3x \\ -3x \\ \hline 0 \\ \end{array} \quad \begin{array}{r} -8 \\ \hline x+1 \end{array}$$

4. $\frac{3x^3 + 9x - 1}{x+2}$

5. $\frac{x+2}{x+1}$

ARN except $x = 0$ $x + 2 + \frac{-8}{x+1}$ ARN except $y = 0$ C ARN except $y = 1$ $3x^3 + 9x - 1$ ARN except $x = 2$

6. What is the remainder when you divide $12x^2 + 17x - 5$ by $3x + 2$?

$$\begin{array}{r} 4x^1 + 3 \\ \hline 3x+2 \left[\begin{array}{r} 12x^2 + 17x - 5 \\ -12x^2 - 8x \\ \hline 9x - 5 \\ -9x - 4 \\ \hline -11 \end{array} \right] \end{array}$$

$$6. \frac{-11}{3x+2}$$

Simplify the expression, if possible.

$$7. \frac{-35x^6}{25x^2} \quad \cancel{(x-2)}$$

$$8. \frac{2x-18}{9-x}$$

$$\boxed{\frac{2(x-9)}{-1(x-9)}}$$

$$9. \frac{2x^2-x-15}{x^2+x-12}$$

$$\begin{array}{r} *AC \\ 2 \cdot -15 \\ \hline -30 \end{array}$$

$$\begin{array}{r} +B \\ -1 \\ \hline -4 \end{array}$$

$$7. \frac{-7x^4}{5}$$

$$\begin{aligned} & (2x^2 - 6x)(+5x - 15) \\ & 2x(x-3)5(x-3) \\ & (2x+5)(x-3) \end{aligned}$$

$$8. \frac{2}{-1} = -2$$

$$\boxed{\frac{(2x+5)(x-3)}{(x+4)(x-3)}}$$

$$9. \frac{2x+5}{x+4}$$

$$10. \frac{x^2-3x-10}{x^2-9x+20}$$

$$\boxed{\frac{(x-5)(x+2)}{(x-5)(x-4)}}$$

$$11. \frac{2x+9}{4x-3}$$

simplified

$$12. \frac{\frac{x^2-16}{x-4}}{-2(x+4)} \cdot \frac{\frac{A}{B}}{\frac{C}{D}} =$$

$$\frac{x^2-16}{x-4} \cdot \frac{1}{-2(x+4)}$$

$$10. \frac{x+2}{x-4}$$

$$\frac{(x+4)(x-4)}{x-4} \cdot \frac{1}{-2(x+4)}$$

$$11. \text{simplified}$$

$$12. \frac{-1}{2}$$

Find the product or quotient.

$$13. \frac{18x^4}{25x^2} \cdot \frac{50x^5}{27x^8} = \frac{900x^9}{(675x^{10})}$$

$$= \boxed{\frac{4}{3x}}$$

$$14. \frac{20}{x^3} \div \frac{30}{x^5} = \frac{20}{x^3} \cdot \frac{x^5}{30}$$

$$= \frac{20x^5}{30x^3} = \boxed{\frac{2x^2}{3}}$$

$$13. \frac{4}{3x}$$

$$14. \frac{2x^2}{3}$$

$\frac{-11}{3x+2}$	$\frac{-7x^4}{5}$	-2	$-\frac{1}{2}$	$\frac{x+2}{x-4}$	$\frac{2x^2}{3}$	$\frac{2x+5}{x+4}$	$\frac{2x+9}{4x-3}$	$\frac{4}{3x}$
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Find the product or quotient.

15. $\frac{4x^3+6x^2}{20x^4-8x^3} \div \frac{2x^2+3x}{45x-18}$

$$\begin{aligned} & \frac{2x^2(2x+3)}{4x^3(5x-2)} \cdot \frac{9(5x-2)}{x(2x+3)} \\ = & \frac{18x^2}{4x^3} = \boxed{\frac{9}{2x}} \end{aligned}$$

16. $\frac{x^2-2x-8}{x^2+5x+6} \cdot \frac{x^2+2x-3}{x^2-8x+7}$

$$\begin{aligned} & \frac{(x-4)(x+2)}{(x+2)(x+3)} \cdot \frac{(x+3)(x-1)}{(x-7)(x-1)} \\ & \boxed{\frac{x-4}{x-7}} \end{aligned}$$

15. ~~$\frac{9}{2x}$~~

16. ~~$\frac{x-4}{x-7}$~~

Solve the equation.

17. $\frac{-5}{x+6} \cancel{x-2} = \frac{x}{x}$

$$\begin{aligned} -5x &= -2(x+6) \\ -5x &= -2x-12 \\ +2x &+2x \\ -3x &= -12 \\ \frac{-3x}{3} &= \frac{-12}{3} \\ x &= 4 \end{aligned}$$

19. $\frac{3x}{2} \cancel{x+6} = \frac{6}{x+3}$

$$3x(x+3) = 12$$

$$3x^2 + 9x = 12$$

$$\frac{3x^2}{3} + \frac{9x}{3} - \frac{12}{3} = 0$$

$$x^2 + 3x - 4 = 0 \quad (x+4)(x-1) = 0$$

$$x+4=0 \quad x-1=0 \quad x= -4 \quad x=1$$

18. $\frac{x}{x-1} \cancel{x-14} = \frac{-14}{x-9}$

$$\begin{aligned} x(x-9) &= -14(x-1) \\ x^2 - 9x &= -14x + 14 \\ +14x &+14x \\ x^2 + 5x - 14 &= 0 \\ + &* \end{aligned}$$

$$(x+7)(x-2) = 0$$

$$\begin{array}{r} x+7=0 \quad x-2=0 \\ -7 -7 \quad +2 +2 \\ x=-7 \quad x=2 \end{array}$$

17. $x=4$

18. $x=2 \frac{1}{4} - 7$

19. $x=-4 \frac{1}{4} 1$

20. You have an 8 pint mixture of paint that is made up of equal amounts of yellow paint and blue paint. To create a certain shade of green, you need a paint mixture that is 80% yellow. How many pints of yellow paint do you need to add to the mixture? You must set up an equation and solve.

total 8 : 4 yellow + blue

$$\frac{\text{yellow}}{\text{total}} : \frac{4+x}{8+x} \cancel{x-0.8}$$

$$1(4+x) = 0.8(8+x)$$

$$4+x = 6.4 + 0.8x$$

$$\frac{-0.8x}{-4+0.2x} = \frac{6.4}{-0.8x}$$

$$0.2x = -4.4$$

$$0.2x = -4.4$$

-7 and 2	-4 and 1	4	$\frac{9}{2x^2}$	$\frac{x-4}{x-7}$	12
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$$\frac{0.2x}{0.2} = \frac{2.4}{0.2}$$

$$\boxed{x=12}$$

20. 12 pints